



Faculty of Engineering

**MODELLING OF REINFORCED CONCRETE BEAM FOR
FLEXURAL BEHAVIOUR**

Lydia Kristen Binti Edward Mongudal

Bachelor of Engineering with Honours
(Civil Engineering)
2005

TA
683.2
L983
2005

UNIVERSITI MALAYSIA SARAWAK

BORANG PENYERAHAN STATUS TESIS

Judul: Modelling of Reinforced Concrete Beam
for Flexural Behaviour


Sesi Pengajian: 2004 - 2005

Saya LYDIA KRISTEN BINTI EDWARD MONGUDAL
(HURUF BESAR)

mengaku membenarkan tesis * ini disimpan di Pusat Khidmat Maklumat Akademik, Universiti Malaysia Sarawak dengan syarat-syarat kegunaan seperti berikut:

1. Tesis adalah hakmilik Universiti Malaysia Sarawak.
2. Pusat Khidmat Maklumat Akademik, Universiti Malaysia Sarawak dibenarkan membuat salinan untuk tujuan pengajian sahaja.
3. Membuat pendigitan untuk membangunkan Pangkalan Data Kandungan Tempatan.
4. Pusat Khidmat maklumat Akademik, Universiti Malaysia Sarawak dibenarkan membuat salinan tesis ini sebagai bahan pertukaran antara institusi pengajian tinggi.
5. ** Sila tandakan () di kotak berkeuaan

- SULIT (Mengandungi maklumat yang berdarjah keselamatan atau kepentingan Malaysia seperti yang termaktub di dalam AKTA RAHSIA RASMI 1972)
- TERHAD (Mengandungi maklumat TERHAD yang telah ditentukan oleh organisasi/badan di mana penyelidikan dijalankan).
- TIDAK TERHAD



(TANDATANGAN PENULIS)

ALAMAT TETAP:
P.O. Box 125,
Kg. Tingkalanon,
Kota Marudu,
Sabah, Malaysia.

Tarikh: 15/4/05

Disahkan oleh:


(TANDATANGAN PENYELIA)

Dr. Ng Chee Khern
Nama Penyelia

Tarikh: 10/5/2005

CATATAN * Tesis dimaksudkan sebagai tesis bagi Ijazah Doktor Falsafah, Sarjana dan Sarjana Muda
** Jika tesis ini SULIT atau TERHAD, sila lampirkan surat daripada pihak berkuasa/organisasi berkenaan dengan menyatakan sekali sebab dan tempoh tesis ini perlu dikelaskan sebagai SULIT dan TERHAD.

This final year project attached here;

Title : Modelling of Reinforced Concrete Beam for Flexural Behaviour

Author's name: Lydia Kristen Binti Edward Mongudal

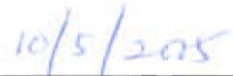
Matrix number: 6765

Has been read and approved by



Prof. Madya. Dr. Ng Chee Khoo

Supervisor



Date

**MODELLING OF REINFORCED CONCRETE BEAM FOR FLEXURAL
BEHAVIOUR**

P.KHIDMAT MAKLUMAT AKADEMIK
UNIMAS



1000143629

LYDIA KRISTEN BINTI EDWARD MONGUDAL

**This Report is Submitted to Faculty of Engineering, Universiti Malaysia
Sarawak in Partial Fulfillment of the Requirements for the Degree of
Bachelor of Engineering with Honours (Civil Engineering) 2005**

Dedicated to beloved Mom and Dad,

Roy, Eva, Becca and Ronn.

ACKNOWLEDGEMENT

Thank GOD for giving me enough time, strengthen me in pain, inspiring and guiding me throughout the completion of this project. For without Him, it is impossible for me to complete this project on time thus successful.

Having this opportunity, I would like to express my highly gratitude to my supervisor, Prof. Madya. Dr. Ng Chee Khoon for the advise, guide and support in order for me to produced a quality report.

Special thanks goes to my beloved mom and dad for their unceasing love, prayer, and financial supports. To my dearly brothers, sisters, relatives, course mate, and friends, I thank God once again for giving me a lovely person like you all. To Miss. Esther Sanggedha Anandaraj, thanks for the guide, prayer, and support in time of need.

I wish finally to express my deep appreciation to all the Faculty of Engineering lecturers, staffs, technicians, especially Mr. Rhyier Juen for allowing me using CATIA Lab in finishing my FORTRAN program.

ABSTRACT

A FORTRAN program for the non-linear analysis of reinforced concrete beam has been developed in this study. This program is able to produce the complete load-deflection behaviour and moment-curvature relationship for the whole flexural response of the beams. The computational results have been verified by manual calculations, indicating that any error in the calculation has been avoided. However, this program is only applicable to simply-supported T-beams with both compression and tension reinforcements.

ABSTRAK

Satu program FOTRAN bagi analisa ketidak linearan rasuk konkrit bertetulang telah dibina dalam kajian ini. Program ini mampu menghasilkan tindakan beban-pemesongan dan hubungan daya-kelengkungan yang lengkap bagi kesemua respons kelenturan rasuk tersebut. Hasil pengiraan telah disahkan melalui pengiraan manual, menunjukkan sebarang kesilapan dalam kiraan telah dielakkan. Walaubagaimanapun, program ini hanya boleh digunakan untuk rasuk-T sokongan-mudah bersama kedua-dua tetulang kemampatan dan ketegangan.

TABLE OF CONTENTS

CONTENT	Page
ACKNOWLEDGMENT	iii
ABSTRACT	iv
ABSTRAK	v
LIST OF TABLES	ix
LIST OF FIGURES	x
LIST OF NOTATIONS	xi
CHAPTER 1 INTRODUCTION	
1.1 General	1
1.2 Historical Development of Reinforced Concrete	1
1.3 Problem Statement	4
1.4 Aim and Objectives	4
1.5 Chapter Overview	5
CHAPTER 2 LITERATURE REVIEW	
2.1 Computers Program and Engineering.	6
2.2 Application of FORTRAN Programming Language in Civil Engineering	8

2.3	Flexural Behavior of Reinforced Concrete beam	9
2.3.1	Load-deflection Response of Concrete Beams	9
2.3.2	Moment-Curvature for Reinforced Concrete Beam	11
2.4	Summary	12
CHAPTER 3 METHODOLOGY		
3.1	Research Modules	13
3.2	Cross Section, Stress and Strain Distribution of Reinforced Concrete Beam	14
3.2.1	Uncracked Sections	15
3.2.2	Cracked Sections	17
3.3	Flexural Analysis of Beams	20
3.4	FORTTRAN Program Design	22
CHAPTER 4 RESULTS AND DISCUSSIONS		
4.1	Beam Model	28
4.2	Manual Computations	28
4.2.1	Computation for Uncracked Section	32
4.2.2	Computation for Cracked Section	35
4.3	Comparison between Manual and FORTRAN Computations Results.	43
4.4	Moment Vs. Curvature	43
4.5	Load-Deflection Behavior	46

CHAPTER 5	CONCLUSIONS AND RECOMMENDATIONS	
5.1	Conclusions	49
5.2	Recommendations	50
REFERENCES		51
APPENDIX: FORTRAN PROGRAM LISTING		52

LIST OF TABLES

Table		Page
1	Partial list of programming languages interest to engineers	7
2	Manual computation results for the total of initial force and initial moment for $C_1 = 96.638\text{mm}$	42
3	Comparison for manual and FORTRAN results	42

LIST OF FIGURES

Figure		Page
1	Load-deflection behaviour of a reinforced concrete beam	10
2	Moment-curvature diagram for a reinforced concrete beam	11
3	Strain and stress distribution of an uncracked beam section	15
4	Strain and stress distribution of a cracked beam section	18
5	Division of segment in the parabolic stress block	18
6	Load-deformation relationship of a beam under two symmetrically placed concentrated loads	21
7	Load-midspan deflection of a reinforced concrete beam	22
8	The Top-down design process	23
9	Flowchart of the FORTRAN program for the beam analysis	25
10	Beam dimensions and reinforcement details	29
11	Distribution of strains and stresses in cracked beam section	36
12	Uncracked beam in the elastic range of loading	43
13	Moment-curvature diagram	47
14	Load-deflection diagram	48

LIST OF NOTATIONS

A_s	-	area of nonprestressed tension reinforcement
A'_s	-	area of compression reinforcement
B_E	-	flange width
B_w	-	web width
C_c	-	concrete compressive force in cross section
C_s	-	steel compressive force in cross section
C_l	-	distance from extreme compression fiber to neutral axis
D_s	-	effective depth, that is, distance from extreme compression fiber to centroid of tension reinforcement
D'_s	-	distance from extreme compression fiber to centroid of compression reinforcement
E_c	-	modulus of elasticity of concrete
E_s	-	modulus of elasticity of reinforcement
H	-	overall thickness of member
H_F	-	flange thickness
F_n	-	the initial force
f_{ct}	-	splitting tensile strength of concrete
f_{cu}	-	specified compressive strength of concrete
f_r	-	modulus of rupture of concrete
f_s	-	calculated stress in reinforcement at service loads

- f_y - specified yield strength of nonprestressed reinforcement
- f_c - cylinder compressive strength of concrete
- I_{cr} - moment of inertia of cracked section transformed to concrete
- I_e - effective moment of inertia for computation of deflection
- I_{EC} - the effective moment of inertia for computation of deflection of cracked T-section
- I_{EUC} - the effective moment of inertia for computation of deflection of uncracked T-section
- I_g - moment of inertia of gross concrete section, neglecting reinforcement
- I_{gt} - moment of inertia of gross transformed uncracked section
- LAM - the lever arm of the compression force from top fibre
- LB - the centre of level of each section
- Ma - applied moment in member
- M_{cr} - cracking moment
- M_n - the initial moment
- n - modular ratio
- P - the axial load
- YB - the level of each section
- Y_C - the centroid for cracked transform of doubly reinforced T-section
- Y_{UC} - the distance from centroid to extreme fiber of the transformed section
- y_b - distance from the centroidal axis to the extreme fibre in tension

y_i	-	distance from the centroidal axis to the extreme fibre in compression
ϵ_c	-	the strain in concrete
ϵ_{ct}	-	the strain
ϵ_s	-	the strain in steel
ϕ	-	the curvature of each cross section
ϕ_c	-	the curvature for cracked T-section
ϕ_{uc}	-	the curvature for uncracked T-section
Δ_c	-	the deflection for cracked T-section
Δ_{uc}	-	the deflection for uncracked T-section
ΣF_n	-	total of the initial force
ΣM_n	-	total of the initial moment

CHAPTER 1

INTRODUCTION

1.1 General

Beam is one of the most common elements in design of reinforced concrete. Concrete beam in nature has a character which is strong in compression and weak in tension. In order to resist the tension, embedded materials, usually in the form steel bars, are provided in the concrete beam. Such combination create reinforced concrete beam. Reinforced concrete beam has the ability to resist both compressive and tensile stresses. If a reinforced concrete beam is designed properly, it can perform well to resist the bending moment due to subjected load applied to the member. Thus, it is essential to study the load-deformation response of a reinforced concrete beam to provide the designer the principles required to apply in the design consideration.

1.2 Historical Development of Reinforced Concrete

Reinforced concrete has been used as building material since last decades

and still preferable nowadays. It is widely used in most countries because of the wide availability of reinforcing bars and economy of concrete constituents such as cement, aggregate and water.

In 1801, Frenchman, F. Coignet has published his statement of principles of construction, recognising the weakness of concrete in tension. He then, published a book illustrating the uses of reinforced concrete in 1861. For the first time, in 1848, another Frenchman, J.L. Lambot construct a rowboat of concrete reinforced with wire for exhibition in the 1855 World's Fair in Paris. His model included drawings of a reinforced concrete beam and a column reinforced with four round iron bars (MacGregor, 1992).

In 1850s, an American lawyer and engineer, Thaddeus Hyatt has carried out an experiment of reinforced concrete beams. He provides longitudinal bars in tension zone and vertical stirrups for shear in his beams. Unfortunately, Hyatt's work was not known until he privately published a book describing his tests and building system in 1877(MacGregor, 1992).

In 1867, J. Monier, owner of French nursery garden, has patented concrete containers reinforced with metal frames for planting trees. His same patent then was used to patent another reinforced concrete structure such as reinforced pipes and tanks (1868), flat plates (1869), bridges (1873), and stairs (1875) (MacGregor, 1992).

Professors Morsch and Bach of the University Of Stuttgart has carried out an experiment to test the strength of reinforced concrete and the method of computing the strength of reinforced concrete was developed Mr. Koenen, chief building inspector for Prussia. He published the first manuscript on the theory and design of concrete structures in 1886. In his book, he presented an analysis which assumed that the neutral axis was at the midheight of the member (MacGregor, 1992).

W.E. Ward, a mechanical engineer built the first reinforced concrete building in the United States in 1875. It was a house built on Long Island. In 1888, E.L. Ransome constructed a building having cast-iron columns and a reinforced concrete floor system consisting beams and slab made from flat metal arches covered with concrete. In 1890, Ransome built the Leland Stanford, Jr. Museum in San Francisco. This two-story building used discarded cable car rope as beam reinforcement. In 1903, he built the first building in the United States completely framed with reinforced concrete in Pennsylvania. In 1906, C.A.P. Turner developed the first flat slab without beams (MacGregor, 1992).

In the last two decades, many books, technical articles, and codes present the theories of mechanical behaviour of reinforced concrete and help the engineer came to understand the principles applied in design procedures. As in 1894, Coignet (son of the earlier Coignet) and de Tedesko extended Koenen's theories to develop the working stress design method for flexure (MacGregor, 1992).

1.3 Problem Statement

Understanding on the behaviour of the reinforced concrete beams has become more important as it is a basis of ideas for designing a reinforced concrete member. Before proceeding to design process, a section should be analyzed to determine if its nominal resisting strength is adequate to carry the load applied to the member. However, because of a large numbers of parameters that should be considered in analysis, such as geometrical width, depth, area of reinforcement, steel strain, concrete strain, steel stress, and so on, computer programs are required to assist the analysis.

This project studies on the flexural behaviour of reinforced concrete beam with a computer model based on section analysis. Non-linear behaviour of materials are seldom considered in computer models, but it will be considered in this study.

1.4 Aim and Objectives

The main aim of this project is to model the flexural behaviour of reinforced concrete beams. Development of this model is made using Fortran 90 program. The flexural resistance will be calculated by using cross section analysis based on force equilibrium and compatibility. Deflection of the beam will be calculated by conjugate beam method based on curvature. Therefore, the load-deflection

response is obtained. All calculation will be based on ACI Building Code (1999).

1.5 Chapter Overview

This project is divided into two parts. The first part consists of three chapters. Chapter 1 gives a brief introduction of reinforced concrete beam. Historical development of reinforced concrete, problem statement, aim and objectives, and chapter overviews are included. Chapter 2 presents computer programming background and reason argument about flexural behaviour of reinforced concrete beam. The method of analysis used in determining the flexural resistance and deflection are discussed in Chapter 3.

In the second part of this project, Chapter 4 gives the case scenario and based on this, the data given will be used in Fortran computation to get the flexural response. After the completion of the computational program, the results both from manual and Fortran computations are discussed. Chapter 5 presents the conclusions indicating the achievement of the aim and objectives of this project and some recommendations for future use.

CHAPTER 2

LITERATURE REVIEW

2.1 Computer Program and Engineering

The computer is the most important invention of the 20th century. A computer is a special type of machine that stores information and can perform mathematical calculations on that information at speeds much faster than human beings can think (Mayo and Martin, 1991). A program, which is stored in the computer's memory, tells the computer what sequence of calculations are required and which information to perform the calculations on.

Engineers and scientists were among the first large-scale computer users dating back to the earliest back of the invention of computers. Engineers use computers in many ways, but the software that they used usually falls into two broad categories. The first contains utilities, such as word processing and graphics programs, that are low-cost packages and require no programming. The second category includes programs devoted specifically to engineering applications. This requires that the engineers to write their own program. Sometimes it is possible to modify an existing program, but some programming is unavoidable. There

are five major uses of computers in engineering such as modelling and simulations, data acquisition, data analysis, process control, and design.

There are various programming languages of interest to engineers. Table 2.1 list some of the programming languages and its strong points (Mayo and Martin, 1991).

Table 2.1: Partial list of programming languages of interest to engineers

Programming Languages	Description
a) FORTRAN	A compiled language widely used for engineering applications. Contains a full range of structured commands and uses of subroutines which promote good style. Periodic revisions update the language to include new advances.
b) BASIC	An interpreted language primarily used for its simplicity. The lack of structured commands tends to produce the problematic spaghetti code. The structure of a subroutine using the GOSUB statement prevents development of long programs. Proprietary dialects, such as QuickBASIC eliminate some of these problems.
c) Pascal	A compiled language which utilizes structured constructs. Promotes good programming practice. Very good for handling nonnumeric data, but somewhat limited for computational work.
d) C	Very powerful compiled language which combines system level and high-level commands. Requires an advanced level of programming experience and can be somewhat difficult to debug. Debugging problems are most severe for lengthy programs.

2.2 Application of FORTRAN Programming Language in Civil Engineering

Programming language has been used in Civil Engineering in a variety of application. Computer program such as ABAQUS, ANSR, and FEAP were written in the FORTRAN computer language for the structural analysis (Austin et al. 1995). These programs offered a restricted, but well implemented, set of numerical linear/nonlinear time-history response calculations.

The LSTRLP algorithm is implemented by an optimization code written in Fortran 90 (Lamberti and Pappalettere, 2003). The optimization code is tested in eight cases of weight minimization of bar truss and frame structures. The Gauss–Legendre method was used for the numerical integration of each of the integrals. The system of non-linear equations (including contributions from all elements) was solved using FORTRAN. A good agreement between experimental and predicted data was obtained (Yamsaengsung and Moreira, 2001). In 2004, ESDU 90002 introduces a FORTRAN program, provided in both compiled and uncompiled forms as ESDUpac A9002, for calculating the flexural buckling strength, and the local and inter-rivet buckling stresses, of uniform section struts.